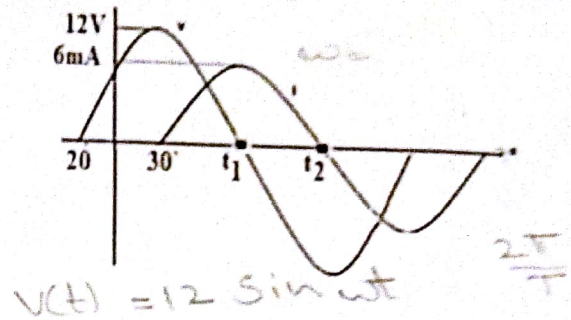


Q1)-

The waveforms of a series AC circuit are shown in the figure.

- Write the mathematical expressions for $v(t)$ and $i(t)$ if the frequency is 60HZ.
- What is the power factor of this circuit?
- Determine the type and value of the elements..



Q2)-

a)-The sinusoidal waveform is $v(t)=60 \sin (377t +20^\circ)$ V , sketch the waveform , and determine

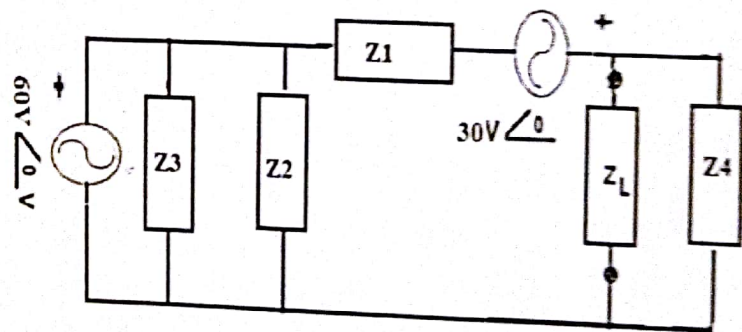
- Average power. *value*
- Effective value.
- The magnitude of the waveform at $t = 6\text{ms}$

Q3)-

For the circuit shown in the figure.

$Z_1=4-J6$, $Z_2= -J6$,
 $Z_3=J4$ and $Z_4=2 \Omega$

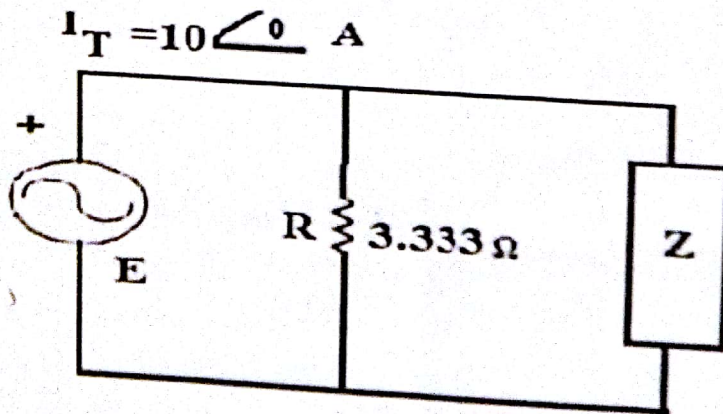
Determine the value of Z_L for maximum power to the Load, and find P_{max} .



Q4)-

For the circuit shown in the figure, the total current leads the source voltage E by 53.13°

- Determine the value of the unknown element.
- find E



داشرة حثية

resistor

Q1

Q1 First we have to determine ω

$$\omega = 2\pi f$$

$$\omega = 2 \times 3.14 \times 60$$

$$\omega = 376.8 \text{ rad/s}$$

$$v(t) = 12 \sin(376.8t + 20^\circ) \text{ V}$$

$$i(t) = 6 \text{ mA} \sin(376.8t - 30^\circ) \text{ A}$$

$$b) P_f = \cos(\theta_v - \theta_i)$$

$$= \cos(20 + 30)$$

$$= \cos 50$$

$$P_f = 0.642 \text{ lagging}$$

$$c) E = \frac{V_m}{\sqrt{2}} = \frac{12}{\sqrt{2}} = 8.485 \angle 20^\circ \text{ V}$$

$$I = \frac{I_m}{\sqrt{2}} = \frac{6 \times 10^{-3}}{\sqrt{2}} = 4.242 \angle -30^\circ \text{ mA}$$

$$Z_t = \frac{E}{I} = \frac{8.485 \angle 20^\circ}{4.242 \angle -30^\circ} = 2 \text{ k} \angle 50^\circ \Omega$$

$$2 \angle 50^\circ = 1.285 \text{ k} + j 1.532 \text{ k} \Omega$$

\therefore the elements are $1.285 \text{ k}\Omega$ resistor and $1.532 \text{ k}\Omega$ inductor

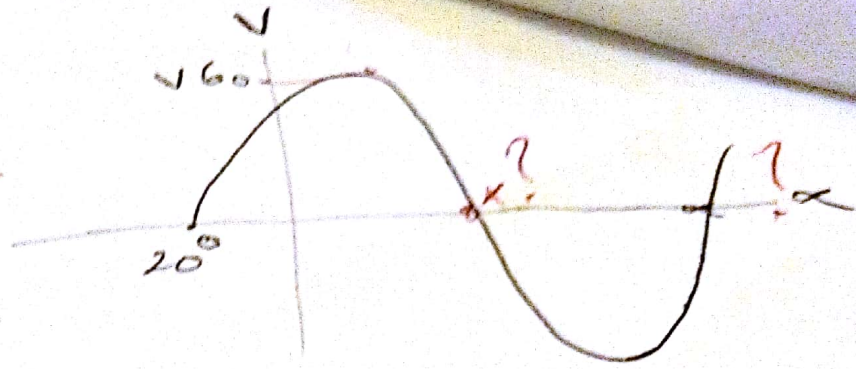
$$L = ?$$

Q2

a

1A

1] the average value
= zero because
the sin wave is identical
wave.



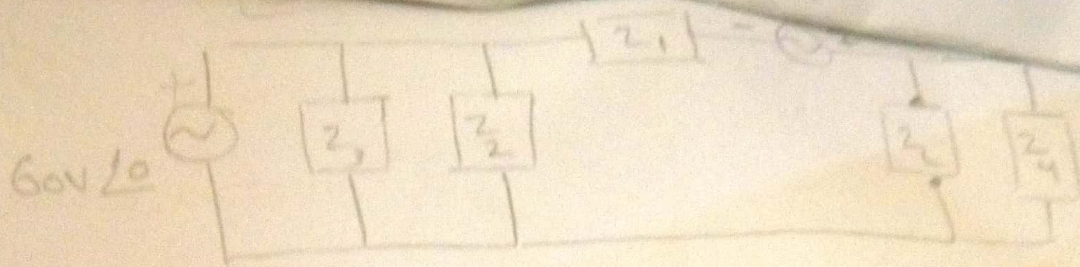
$$V_{\text{eff}} = \frac{V_m}{\sqrt{2}} = \frac{60}{\sqrt{2}} = 42.426 \text{ V}$$

$$3] v(t) = 60 \sin(377t + 20^\circ) \text{ V}$$

$$\begin{aligned} v(6\text{ms}) &= 60 \sin(377 \times 6 \times 10^{-3} + 20^\circ) \text{ V} \\ &= 60 \sin\left(2.262 \times \frac{180^\circ}{\pi} + 20^\circ\right) \text{ V} \\ &= 60 \sin(129.668^\circ + 20^\circ) \text{ V} \\ &= 60 \sin(149.668^\circ) \text{ V} \end{aligned}$$

$$\therefore v(6\text{ms}) = 30.3 \text{ V}$$

Q3)



$$Z_1 = 4 - j6 = 7.211 \angle -56.309^\circ$$

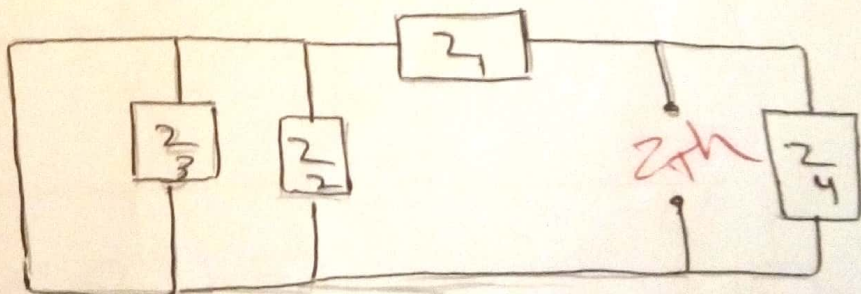
$$Z_2 = -j6 = 6 \angle -90^\circ$$

$$Z_3 = j4 = 4 \angle 90^\circ$$

$$Z_4 = 2 = 2 \angle 0^\circ$$

by using thevenin's theory

$$Z_{th} = Z_1 \parallel Z_2$$



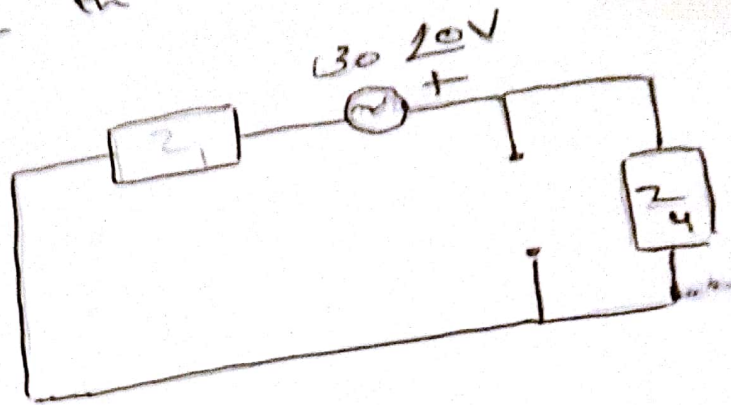
$$Z_{th} = \frac{7.211 \angle -56.309^\circ \times 2}{6 - j6} = \frac{14.422 \angle -56.309^\circ}{8.485 \angle -45^\circ}$$

$$Z_{th} = 1.699 \angle -11.309^\circ \Omega = 1.666 - j0.333 \Omega$$

$$Z_L = Z_{th}^* = 1.699 \angle 11.309^\circ \Omega = 1.666 + j0.333 \Omega$$

$$\underline{E}_{th}^+$$

30∠0° V Source active E_{th}^+

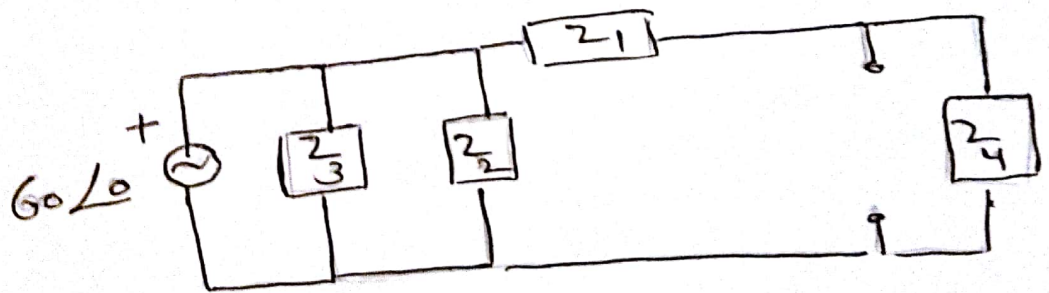


$$E_{th}^+ = E_{Z_4}$$

by using VDR

$$E_{th}^+ = \frac{30 \angle 0^\circ \times 2}{8.485 \angle -45^\circ} = 7.071 \angle 45^\circ \text{ V} = 5 + j5 \text{ V}$$

60∠0° Source active E_{th}^+



$$E_{th}^+ = E_{Z_4}$$

$$E(Z_1 + Z_4) = E_{source}$$

$$E_{th}^+ = \frac{60 \angle 0^\circ \times 2}{8.485 \angle -45^\circ}$$

$$E_{th}^+ = 14.142 \angle 45^\circ \text{ V} = 10 + j10 \text{ V}$$

$$E_{th} = E_{th}^{\prime} + E_{th}^{\prime\prime}$$

$$= 15 + j15 = 21.213 \angle 45$$

$$P_{max} = \frac{E_{th}^2}{4Z_{th}} = \frac{(21.213)^2}{4 \times 1.699} = 66.214 \text{ watt}$$

Q_{11}

$$I = 10 \angle 0^\circ \text{ A}$$

$$E = E \angle -53.13^\circ \text{ V}$$

$$P_f = \frac{G}{Y_t}$$

→ because Z contains a single element
and the circuit has capacitive
effect

$$\cos 53.13 = \frac{0.3}{Y_t}$$

$$Y_t = \frac{0.3}{0.6} = 0.5$$

$$Y_t = 0.5 \angle 53.13$$

$$Y_t = 0.3 + j0.399$$

$$Y_t = 0.3 + j0.4$$

$$Y_t = \underbrace{3\mu}_R + \underbrace{2.5\mu}_{XC}$$

$$E = \frac{I}{Y_t} = \frac{10}{0.5} = 20 \text{ V}$$

the unknown element is a capacitor with a value of
2.5 μ